

Practice Worksheet: Synthetic Division

Complete each statement to make it true.

- 1] If $g(-4) = 0$, then _____ is a factor of $g(x)$.
- 2] $(x^4 - 3x^2 + 2x - 5) \div (x^2 - 2x + 3)$ can NOT be done using _____ division.
- 3] If $f(5) = 3$, then $f(x) \div (x - 5)$ has a _____ of 3.

Use the Remainder Theorem to find the remainder when dividing each by $(x - 3)$. Is it a factor?

- 4] $f(x) = x^3 - 5x^2 - 3x + 9$ 5] $g(x) = x^3 + 2x^2 - 6x + 12$ 6] $h(x) = x^3 - x^2 - 7x + 3$

Use the Factor Theorem to determine if the divisor is a zero of the original polynomial. If so, rewrite as a product of two factors.

$\begin{array}{r rrrr} -1 & 1 & 2 & -1 & -2 \\ & & -1 & -1 & 2 \\ \hline & 1 & 1 & -2 & 0 \end{array}$	$\begin{array}{r rrrr} 4 & 3 & -10 & 0 & -5 \\ & & 12 & 8 & 32 \\ \hline & 3 & 2 & 8 & 27 \end{array}$	$\begin{array}{r rrrrr} -2 & 1 & 2 & 1 & 5 & 6 \\ & & -2 & 0 & -2 & -6 \\ \hline & 1 & 0 & 1 & 3 & 0 \end{array}$
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Using the synthetic division provided, write the original polynomial in both standard form and factored form. Then, sketch the graph.

$$10] \begin{array}{r|rrrrr} 4 & -1 & 10 & -24 & -32 & 120 \\ & \downarrow & -4 & 24 & 0 & -120 \\ \hline & -1 & 6 & 0 & -32 & \\ 4 & & \downarrow & -4 & 8 & 32 \\ \hline & -1 & 2 & 8 & 0 & \\ -2 & & \downarrow & 2 & -8 & \\ \hline & -1 & 4 & 0 & & \end{array}$$

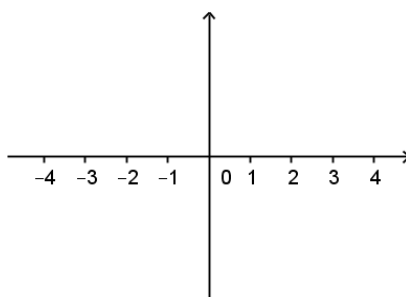
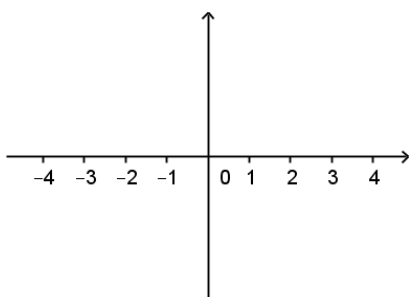
Standard Form:

Factored Form:

$$11] \begin{array}{r|rrrrr} -3 & 1 & 3 & -2 & -6 & 1 & 3 \\ & \downarrow & -3 & 0 & 6 & 0 & -3 \\ \hline & 1 & 0 & -2 & 0 & 1 & 0 \\ -1 & & \downarrow & -1 & 1 & 1 & -1 \\ \hline & 1 & -1 & -1 & 1 & 0 & \\ -1 & & \downarrow & -1 & 2 & -1 & \\ \hline & 1 & -2 & 1 & 0 & & \\ 1 & & \downarrow & 1 & -1 & & \\ \hline & 1 & -1 & 0 & & & \end{array}$$

Standard Form:

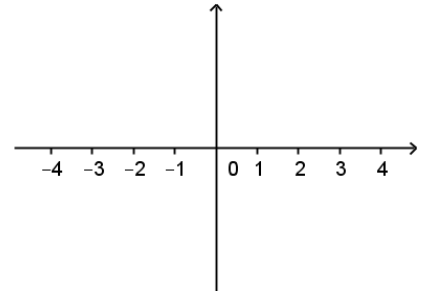
Factored Form:



A polynomial $f(x)$ and one or more factors of $f(x)$ are given. Factor completely using synthetic division and rewrite in factored form. Then sketch the graph. Show all work.

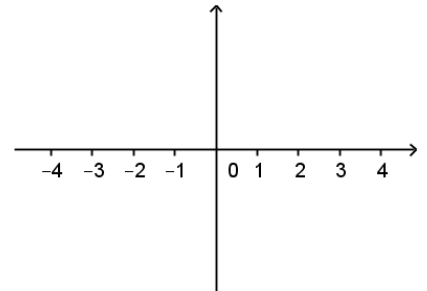
12] $f(x) = -x^3 - 3x^2 + 6x + 8$ has factors of $(x - 2)$ and $(x + 1)$.

Factored form:



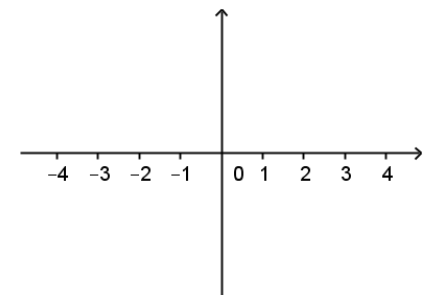
13] $f(x) = 2x^3 - 3x^2 - 14x + 15$ has factors of $(x - 1)$ and $(x - 3)$.

Factored form:



14] $f(x) = x^4 - 7x^3 + 9x^2 + 27x - 54$ has a factor of $(x - 3)$ with multiplicity 3.

Factored form:



15] $f(x) = x^4 - 11x^2 - 18x - 8$ has a factor of $(x + 2)$ and $(x + 1)$ with multiplicity 2.

Factored form:

