

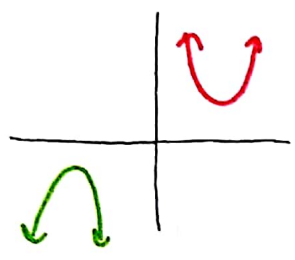
Objective: To apply operations of complex numbers and solve quadratic equations with complex solutions

Complex numbers

real numbers  
( $\frac{1}{2}, 0.25, -4, 5$ )

imaginary numbers  
( $3i, -2i$ )

combinations of both  
( $3+4i$  or  $2-3i$ )



No x-intercepts, but there are zeros/roots that are imaginary

$$\sqrt{x^2} = \sqrt{-1}$$

$$x = \pm i$$

$$\sqrt{-1} = i$$

$$\sqrt{-4} = i\sqrt{4} = 2i$$

$$\sqrt{-75} = i\sqrt{75} = i\sqrt{25 \cdot 3} = 5i\sqrt{3}$$

Examples: simplifying powers of i

$$i^{25} = i$$

$$\begin{array}{r} 6 \\ 4 \overline{)25} \\ \underline{-24} \\ 1 \end{array} \rightarrow \text{new power}$$

$$i^1 = i$$

$$i^{16} = 1$$

$$\begin{array}{r} 4 \\ 4 \overline{)16} \\ \underline{-16} \\ 0 \end{array} \rightarrow \text{new power}$$

$$i^0 = 1$$

Divide the power by 4 and use the remainder as the new power.

$$i^{34} = -1$$

$$\begin{array}{r} 8 \\ 4 \overline{)34} \\ \underline{-32} \\ 2 \end{array} \rightarrow \text{new power}$$

$$i^2 = -1$$

$$i^2 = -1$$

- $i^0 = 1$
  - $i^1 = i$
  - $i^2 = -1$
  - $i^3 = i^2 \cdot i = -i$
- 4 possible answers when simplifying powers of i

complex numbers in standard form :  $\boxed{a + bi}$   
 $\boxed{a - bi}$

operations of complex numbers :

Add/subtracting: combining like terms

$$1.) \underbrace{(-3 + 4i) + (2 - 3i)}_{(-3 + 2) + (4i - 3i)} \\ -1 + i \\ \boxed{-1 + i}$$

$$2.) \overbrace{(-5 - 2i) - (4 + 5i)}^{-5 - 2i - 4 - 5i} \\ \boxed{-9 - 7i}$$

Multiplying: FOIL

$$3.) \underbrace{(2 + 4i)} \underbrace{(3 - 6i)} \\ 6 - 12i + 12i - 24i^2 \\ 6 - 24(-1) \\ 6 + 24 = \boxed{30}$$

\* Remember the fact  
 $i^2 = -1$

$$4.) \underbrace{(-3 - 5i)} \underbrace{(2 + 7i)} \\ -6 - 21i - 10i - 35i^2 \\ -6 - 31i - 35(-1) \\ -6 - 31i + 35 \\ \boxed{29 - 31i} \rightarrow \text{complex number}$$

Solving quadratics with complex solutions.

$$1.) \quad (x-3)^2 + 4 = -8$$

square root Method

$$\frac{-4 \quad -4}{\sqrt{(x-3)^2} = \sqrt{-12}}$$

Remember  $\oplus$

$$x-3 = \pm \sqrt{-12}$$

$$\frac{+3 \quad +3}{x = 3 \pm \sqrt{-12}}$$

$$x = 3 \pm \sqrt{-12}$$

take out (-) as an  $i$

$$\sqrt{-1} = i$$

$$x = 3 \pm i\sqrt{12}$$

$$x = 3 \pm i\sqrt{4 \cdot 3}$$

$$\boxed{x = 3 \pm 2i\sqrt{3}}$$

$$x = 3 + 2i\sqrt{3} \quad x = 3 - 2i\sqrt{3}$$

$$2.) \quad x^2 + 4x + 29 = 0$$

Not factorable

$$\frac{-29 \quad -29}{x^2 + 4x + (2)^2 = -29 + 4}$$

$$\sqrt{(x+2)^2} = \sqrt{-25}$$

completing square

$$x+2 = \pm \sqrt{-25}$$

$$\frac{-2 \quad -2}{x = -2 \pm \sqrt{-25}}$$

quadratic formula

$$x = -2 \pm \sqrt{-25}$$

$$x = -2 \pm i\sqrt{25}$$

$$x = -2 \pm 5i$$

$$\boxed{x = -2 + 5i}$$

$$\boxed{x = -2 - 5i}$$